

1 A review and enhancement of Chapter 7 of AMS Monograph 58:
2 “Secondary Ice Production: Current State of the Science and Future Recommendations”

3 by Field et al. 2017

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6
7 Abstract

8
9 This review consists of three elements: 1) reprising the Hallett-Mossop process and why
10 it cannot explain, of itself, high ice particle concentrations in Cumulus clouds with slightly
11 supercooled tops; 2) a review of the contents of Chapter 7 consisting of selected quotes followed
12 by comments, similar to a formal manuscript review; corrections that should have been caught
13 before Chapter 7 went to press.

14 Literature that was uncited in Chapter 7 that might have altered, and in some cases,
15 enhanced some of the authors’ conclusions, is discussed.

16
17 1. Introduction

18 Field et al. (2017, hereafter, F2017) have done a remarkable job of summarizing a vast
19 amount of work on the continuing enigma of the origin of ice-in-clouds. Not surprisingly,

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20 considering the abundance of publications in various journals relevant to this mystery, some
21 publications were overlooked that might have helped the reader, and altered some of the
22 conclusions wrought in F2017. This review is meant to “fill in” those blanks; to be an
23 enhancement of Chapter 7 rather than a series of criticisms. It is restricted to the cloud
24 microphysical portions of Chapter 7 concerned with ice multiplication in Cumulus clouds, the
25 writer’s specialty.

26 The “embarrassment of citation riches” to much of our prior University of Washington
27 work², is much appreciated. Nevertheless, since it is not possible to be cited too many times,
28 only too few, we dredge up even more of our work relevant to the question of secondary ice that
29 went uncited. The comments contained in this review will range from picayunish errors in
30 F2017 (left until the end) to more significant commentary concerning the workings of the H-M
31 process at the beginning of this review. This is followed by quotes in F2017 followed by
32 comments, a style mimicking that of a pre-publication review, one that I wish I had participated
33 in.

34 We start with a summary of the Hallett-Mossop riming-splintering process (Hallett and
35 Mossop 1974; Mossop and Hallett 1974, hereafter “H-M”) and why the H-M process cannot, of
36 itself, account for the “rapid” development of ice in clouds that F2017 mentions in their abstract.
37 In reading Field et al. it was felt that this distinction between clouds that produce ice rapidly and
38 the inability of the H-M process alone to do that in slightly supercooled Cumulus clouds,
39 beginning with primary ice nuclei (IN) was not made clear.

² Hobbs and Rangno 1985, 1990, and 1998, hereafter HR85, HR90, and HR98, and Rangno and Hobbs 2001 and 2005, hereafter RH2001 and RH2005.

40 Relevant literature that was not cited or possibly not known about by F2017 is indicated
41 by an “u” after the citation in this review, for “uncited.” ‘

42 2. Review of F2017

43 The rapid development of precipitation in Cumulus clouds transitioning to
44 Cumulonimbus clouds, has been noted for many decades via radar (e.g., Battan 1953; Saunders
45 1965, Zeng et al. 2001) and by aircraft (e.g., Koenig 1963). A process that can explain such
46 rapid transitions in clouds whose tops reach much above the freezing level must act very quickly
47 (<10min) to enhance concentrations of ice particles in such clouds. The H-M process is one that
48 is usually cited in conjunction with this rapid formation of ice. However, of itself, even when the
49 broad droplet spectra is satisfied in a Cumulus turret with a top at -8°C with only primary ice
50 nuclei (IN) as ice initiators, such a cloud can never attain the 10s to 100s of ice particles per liter
51 associated with “ice multiplication”, those in modest Cumulonimbus clouds.

52 Why can’t the H-M process alone produce significant ice in Cumulus clouds when its
53 criteria are satisfied?

54 The lifetime of Cumulus turrets is too short, <20 min (e.g., Workman and Reynolds
55 1949u, Braham 1964u, Saunders 1965u). Its too short for several cycles of splinters to develop,
56 those having to reach fast-falling graupel sizes to be significant splinter producers, starting with
57 ice particles from the very few primary ice nuclei (IN) at -8°C. Even the H-M droplet spectra
58 itself is doomed within a few minutes in the lives of ordinary Cumulus turrets as they fall back
59 and evaporate³. Mason’s (1996) calculations, using reasonable assumptions, required 1 h for ice

³ Exceptions might be those situations where fresh turrets rise up through remains of turrets in calm or nearly calm situations.

60 particle concentrations to reach 100 l^{-1} after starting from primary IN, which Mossop noted was
61 untenable for a Cumulus turret. Chisnell and Latham (1976) understood this: “Firstly there are
62 some reported multiplication rates, 10 in 8 min (Mossop *et al.* 1970), 500 in 5 ~ min (Koenig
63 1973-*sic*), which are inexplicable in terms of a 'riming only' model, but which are consistent with
64 a model containing rain drops.”

65 . Absent larger ($>30 \mu\text{m}$ diameter) droplets and/or precipitation-sized drops ($\geq 100 \mu\text{m}$
66 diameter), tens of minutes to an hour or more is required to raise ice particle concentrations from
67 from primary IN concentrations to 100 l^{-1} (e.g., Chisnell and Latham 1976, “Model A”, Mossop
68 1985a,u, Mason 1996), times that are not tenable considering the short lifetimes of Cumulus
69 turrets.

70 Moreover, air translates through Cumulus clouds analogous to lenticular clouds though at
71 a far slower pace (e.g., Malkus 1952u, Asplinden et al 1978u). Thus, while a Cumulus cloud can
72 appear to exist for tens of minutes, its individual turrets cannot. Any splinters that might be
73 formed by a round of very sparse graupel due to primary IN, should an ice crystal have time to
74 become a graupel particle, will go out the side or evaporate as the top declines and evaporates
75 toward the downwind side as illustrated in Byers (1965u, Figure 7.3). One of the lessons learned
76 in the HIPLEX seeding experiments when dry ice, dropped like graupel into supercooled
77 Cumulus turrets, was that it produced ice crystals that drifted out the side of decaying cloud
78 portions (Cooper and Lawson 1984u).

79 Mossop (1985a,u) himself had trouble explaining the rapidity of ice development in his
80 own Cumulus clouds in the Australian Pacific. Using his measured concentrations of frozen
81 drizzle drops as an accelerator of ice formation, Mossop calculated that it would take about 47
82 minutes to go from initial ice concentrations due to primary IN (0.01 per liter) at -10°C to 100

83 ice particles per liter. Mossop knew that this amount of time was untenable for a Cumulus turret.
84 He then reasoned that IN must be about 10 times higher at -10°C to explain that discrepancy, or
85 about 0.1 per liter, to bring the glaciation time he observed down to about 20 minutes
86 (calculating that the concentrations of ice particles increased 10 fold each 10 min beginning with
87 0.1 IN per liter active at -10°C). The concentration of IN surmised by Mossop (1985a, u) is now
88 close to that in updated concentrations of IN by DeMott et al. 2010 of about 0.3 per liter active at
89 -10°C ⁴.

90 However, IN need to be about 10-100 times higher than Mossop's estimate of 0.1 per
91 liter to bring down the time of glaciation to that observed in clouds like his own Australian
92 clouds, namely, ones containing copious droplets >30 μm diameter and some precipitation-sized
93 drops. This was demonstrated by Crawford et al. 2012's case of 100 times the DeMott et al.
94 primary IN with a model cloud top at -10°C , a case study that best mimicked the near-
95 spontaneous glaciation of real clouds having modestly supercooled tops and containing drops
96 >30 μm diameter (often with drizzle or raindrops).

97 In sum, if the droplet spectra does not broaden considerably farther so that droplets larger
98 than 30-40 μm in diameter are in plentiful concentrations (past the Hocking and Jonas 1971;

⁴ It is interesting to note that aufm Kampe and Weickmann (1951) produced virtually the same ice nuclei activity graph as found in DeMott et al. 2010. Also noteworthy is that Blanchard (1957) also using outside air in a city environment as did aufm Kampe and Weickmann, could freeze giant raindrops in a vertical wind tunnel at the same temperatures that this occurs in natural clouds.

99 Jonas 1972) thresholds for collisions with coalescence to begin, there will be no “rapid”
100 glaciation in slightly to modestly supercooled clouds that only meet the H-M droplet spectra
101 criteria.

102 3. Descriptions of ice multiplication in literature uncited by F2017

103 Our follow up studies of ice development in Cumulus and small Cumulonimbus clouds
104 after HR85 and HR90 went uncited in F2017. Those were Rangno and Hobbs 1991u and 1994u,
105 hereafter RH91u and RH94u. We offer a brief summary of our findings before moving on to
106 other relevant uncited findings. We believe that these uncited papers, *en toto*, cast additional
107 light the nature of the problem posed by ice multiplication.

108 a. Discussion of RH91u with some background on HR85

109 In our prior study of ice-in-clouds, HR85, only a 6 s time resolution was available for
110 data during most of the sampling period (1978-1984). Therefore, we sampled rather wide cloud
111 complexes to get meaningful statistics. In addition, our 2-DC probe was only operated
112 sporadically, not continuously in cloud.

113 In RH91u data resolution was 1 s or less, and there was continuous 2-DC coverage of
114 cloud penetrations. Moreover, we carried a vertically-pointable (up or down), mm-wavelength
115 radar, perhaps the first cloud research aircraft to do so.

116 We often sampled much smaller clouds than in HR85 and we found that maritime, short-
117 lived (<1 km wide) “chimney” Cumulus clouds whose tops fell back into warmer air and
118 evaporated, did not produce much *detectable* ice even if they reached close to -10°C. This was
119 true even as their wider, nearby brethren with the same cloud top temperature produced “anvils
120 of ice”, replicating the findings in HR85 (see RH91u, Figure 1). The low ice concentrations

121 found in chimney Cumulus clouds could also have been due to not being able to sample very
122 small ice crystals, those below about 100 μm in maximum dimension. It forced us to reconsider
123 the role of evaporation that we posited was important in the production of ice in HR85.

124 The finding in RH91u that wider clouds had considerably more ice corroborated Mossop
125 et al.'s 1970 and Schemenauer and Isaac's (1984u) earlier findings that cloud width had a
126 profound effect on the development of ice in clouds. These findings implicitly address the
127 importance of the duration of cloud and precipitation-sized drops, if any of the latter, at lower
128 temperatures.

129 Of note is that the maritime Cumulus clouds in Washington State coastal waters during
130 onshore flow are virtually identical to those studied by Mossop and his colleagues in the
131 Australian Pacific in terms of cloud base temperatures, droplet concentrations, ice particle
132 concentrations and in the minimum cloud top temperatures at which most sampling took place
133 (e.g., Mossop et al 1968u, Mossop and Ono 1969u). Our studies were, thus, an attempt at
134 replicating the findings of Mossop and his colleagues without going to Australia.

135 In RH91u, we found again, as noted in F2017, that Mossop's (1985a, u) report that ice
136 concentrations required 20 min to rise from 0.1 per liter to 100 per liter, was still too great an
137 amount of time to account for the rapidity of the glaciation that we observed in our Washington
138 clouds. Lawson et al. (2015) have arrived at a similar conclusion recently though in a different
139 way.

140 In RH91u we also compared the explosive formation of ice in our maritime Cumulus to
141 our prior dry ice cloud seeding experiments (Hobbs 1981u) and again in RH94u. The imagery is

142 remarkably similar as a demonstration of the rapidity, the virtually spontaneous formation of
143 ice⁵. We thought that an important comparison.

144 We also investigated the ocean's influence on ice formation by sampling small to
145 medium Cumulus clouds that developed out of clear air in an extremely cold⁶, offshore flowing
146 air mass over the Washington State coastal waters. Cloud bases were -18°C and cloud tops of
147 the deepest Cumulus, -26°C. The sea surface was roiled by estimated 25-40 kt winds with
148 widespread whitecaps. Mixing from the sea surface, about 13°C, to cloud bases was extreme, as
149 marked by the heavy turbulence on that flight and vomiting. We sampled those cumuliform
150 clouds as they deepened downwind as far as 100 km offshore that day.

151 That day stood out in our studies. We measured the lowest ice particle concentrations in
152 all our sampling of cumuliform clouds with top temperatures -24°C to -26°C by measuring
153 maximum concentration of only 7 l^{-1} in clouds up to about 1 km in depth. This day forced us to
154 conclude that the coastal waters of Washington State, anyway, were not a source of high
155 temperature ice nuclei, counter to some more recent work (DeMott et al. 2016). However, we
156 did not measure concentrations of ice particles that were $< 100 \mu\text{m}$ in maximum dimension.

157 The droplet spectra in those offshore flowing clouds was narrow, as would be expected
158 with such low base temperatures, and again the idea that droplet sizes control ice formation was
159 once again realized by these low concentrations of ice.

⁵ We also found it difficult to arrive at that moment of “explosive” ice development with our aircraft.

⁶ The Quillayute, WA, rawinsonde 500 mb temperature was -45°C the morning of our flight!

160 In sum, from our attempts at replicating Mossop's results in clouds identical to his over
161 many years, we found several departures in ice formation from the operation of the H-M process
162 as it was being described. These discrepancies are somewhat different than those quoted for our
163 research in F2017, hence we reprise them here:

- 164 • The formation of ice was far more rapid in clouds with tops between -5°C and -12°C than
165 could be accounted for by H-M, requiring ≤ 10 min, as judged from the small size of the
166 ice particles in high concentrations, ones that had not yet had time to begin forming
167 aggregates; moreover, they were usually coincident with relatively high LWC that had
168 not had time to be depleted (e.g., HR90, RH91u). Newly risen turrets full of LWC could
169 be seen to transition to an icy, fraying, soft, cotton-candy appearance in less than 10 min.
170 What cloud observer hasn't seen this behavior?
- 171 • Our maritime clouds had very low concentrations of small (≤ 13 μm diameter) droplets
172 once appreciably above cloud base and into the H-M temperature zone. Low
173 concentrations of small droplets were once thought to be an impediment to riming and
174 splintering (e.g., Mossop 1978u; Hallett et al. 1980u), though later studies deemed them
175 to have only a "secondary role" (Mossop 1985b).
- 176 • Measured graupel concentrations, despite our "optimizations" (using high concentrations
177 over a few meters rather than turret-averaged) to try to make H-M work in RH91u were
178 still not high enough to account for the high concentrations of ice particles that developed
179 so quickly.
- 180 • Our fast-glaciating, modest Cumulus and Cumulonimbus clouds with tops between -5°C
181 $\geq -12^{\circ}\text{C}$ did not contain mm-sized raindrops, thought to be critical for rapid glaciation as
182 asserted by F2017. However, copious large droplets (≥ 30 μm diameter) and drizzle-sized

183 drops up to about 500 μm diameter were always found, though the latter in relatively low
184 concentrations^{7,8}. Drop sizes between 30 μm and 60 μm diameter, deemed an important
185 player in ice multiplication by Ono (1972u), were always copious.

186 b. Discussion of RH94u

187 The focus of RH94u was to remove the effects of the H-M process by studying ice
188 development continental and semi-continental clouds found mostly east of the Cascade
189 Mountains of Washington State, clouds that did not meet the H-M criteria. We believed that this
190 was an important next step. The clouds we sampled almost always had base temperatures of 0°C
191 or lower. Droplet concentrations were semi-continental to “continental” ranging from 300 cm^{-3}
192 to 1500 cm^{-3} , many times higher than droplet concentrations in the Washington coastal waters in
193 onshore flow that averaged but $\sim 50 \text{ cm}^{-3}$. Thus, the droplet spectra in the eastern Washington
194 and other cold clouds we sampled were considerably narrower than in our coastal clouds, and
195 due to those cold bases, contained few if any drops meeting the large droplet size ($\geq 23 \mu\text{m}$) in
196 the H-M temperature zone. We again carried our vertically-pointable, mm-radar to help
197 elucidate cloud structures below or above the aircraft.

198 Our findings for the eastern Washington State clouds, simply explained, were that the
199 higher the cloud base temperature, the greater the ice at in a Cumulus cloud, holding cloud top

⁷ We note that in the cloud studied by Mossop (1985u) a drop of 1.5 mm diameter was encountered.

⁸ If Ono (1972u) was correct about the importance of drops between 30 μm and 60 μm diameter, then we may have been barking up the wrong “ice tree” by concentrating on drizzle and raindrop sizes.

200 temperature constant. Thus, a cloud with a base of -15°C and a top of -20°C had far *less* ice than
201 a cloud with a base of 0°C and a top at -20°C with no contribution from H-M. This finding
202 spoke to, as we believed then and continue to believe, the largest droplet sizes of the spectra as
203 being a critical parameter in the production of ice. We continued to find that a measure of the
204 broadness of the FSSP-100-measured droplet spectrum (our “threshold diameter”, or large end
205 “tail” of the droplet spectrum, e.g., HR85) in newly risen turrets lacking much ice ($\leq 1 \text{ l}^{-1}$)
206 continued to be strongly predictive of later maximum ice particle concentrations.

207 We also found that for very cold based clouds ($\leq -8^{\circ}\text{C}$) that Fletcher’s (1962u) summary
208 ice nucleus curve predicted ice concentrations associated with a range of cloud top temperatures
209 extremely well ($r=0.89$). This probably indicated that we had little contribution from probe
210 shattering artifacts after accounting for them (see RH91u). The crystal types in those clouds
211 were almost all delicate stellar and dendritic forms where shattering artifacts would be expected
212 to be rampant⁹.

213 Too, ice formation in the eastern Washington State clouds, as it was in our maritime
214 clouds, was extremely rapid, explosive, in turrets with larger droplets ($\geq \sim 25 \mu\text{m}$ in diameter) as
215 they reached their peak heights with no contribution from H-M. As with our maritime clouds,
216 the scenario of a few much larger particles (graupel) appeared to be coincident with wholesale
217 formation of high ice concentrations.

⁹ While tedious, we inspected all our 2-D imagery in our Cumulus studies for artifact problems;
we didn’t just crunch numbers without looking at every 2-D strip!

218 This did not happen, however, in very cold-based ($\leq -8^{\circ}\text{C}$), shallow clouds with small
219 ($\sim \leq 20$ μm diameter) droplets and tops down to -27°C where ice appeared to form from a
220 “trickle” process likely due to ambient IN concentrations rather than aided by other factors.

221 Too, our evaluation of the H-M process could not explain the ice multiplication that
222 occurred in those few eastern Washington clouds that did meet the H-M criteria. In our
223 calculations we used a “relaxed” FSSP-100 spectra (as lately invoked by Crawford et al. 2012)
224 that resulted in more >23 μm diameter droplets than were actually observed in our calculations to
225 no avail in an attempt to “break” our conclusions (as good scientists do).

226 Two very short but illuminating papers were published in 1998 that discussed two
227 viewpoints concerning the H-M process. Blyth and Latham (1998u) “Commented” on the
228 University of Washington findings² as completely explicable due to the H-M process, counter to
229 the conclusions stated in our papers in which we felt that H-M might be playing a lesser role.
230 We defended our findings in our reply (Hobbs and Rangno 1998u)¹⁰.

231 Following Mossop’s (1978) nomogram for ice development and ice multiplication
232 boundaries given cloud base temperatures¹¹, we evaluated the onset of ice based on cloud depth
233 and temperature of the onset of ice in Cumulus clouds using cloud base temperatures for
234 continental clouds in Rangno and Hobbs (1988u), updated with many more data points from

¹⁰ This colloquy also emphasized an extremely important point in science; we should speak out on findings that we question instead of remaining on the sidelines. We admired Blyth and Latham for questioning our work. After all, we could be wrong!

¹¹ Isaac and Schemenauer (1979), however, criticized Mossop’s 1978 nomogram; Mossop (1979) responded politely with more supportive data.

235 various locations around the world in Rangno and Hobbs 1995u (Figure 12). These data, for
236 non-severe convection, point to a critical role of droplet sizes as proxied by cloud depth for the
237 onset of ice in clouds (as Ludlam 1952) first noted), and, thus when ice multiplication can be
238 expected.

239 c. Other uncited findings that impact F2017

240 Perhaps the most remarkable instance of “secondary” ice formation was left out of the
241 field studies described by F2017: that of Stith et al 2004u in clean tropical updrafts. Stith et al.
242 reported tens of *thousands* per liter of spherical ice particles in tropical updrafts that led to nearly
243 complete glaciation by -12°C and total glaciation by -17°C. As Stith et al. pointed out, and was
244 obvious, there is no mechanism presently known that can explain those observations. The
245 remarkable findings of Stith et al. should have been “front and center” in F2017. (Or, it should
246 have been called out as bogus in a footnote.)

247 Another finding, one that resembles the findings of Stith et al. 2004u, and is also
248 inexplicable by H-M, is that of Paluch and Breed (1984u). High ice particle concentrations (100
249 l⁻¹) formed in a Cumulus cloud updraft at moderate supercooling.

250 Other examples of H-M “exceptionalism” that went uncited in F2017: Cooper and
251 Saunders 1980u, Cooper and Vali 1981u, Gayet and Soulage 1982u, Waldvogel et al 1987u.

252 =====

253 4. A line-by-line critique of F2017, analogous to a pre-publication manuscript review.

254 P7.1: F2017, their introduction: “Airborne observations of ice crystal concentrations are often
255 found to exceed the concentration of ice nucleating particles (INPs) by many orders of

256 magnitude (see, e.g., Mossop 1985; Hobbs and Rangno 1985; Beard 1992; Pruppacher and Klett
257 1997; Hobbs and Rangno 1998; Cantrell and Heymsfield 2005; DeMott et al. 2016). In the 1970s
258 (Mossop et al. 1970; Hallett and Mossop 1974) the discrepancy between expected ice particle
259 concentrations formed through primary ice nucleation and observed ice particle concentration
260 motivated the search for mechanisms that could amplify primary nucleation pathways.”

261

262 While it was gratifying to have our work cited in the Introduction of F2017, the
263 observations of unexpectedly high ice particle concentrations at slight supercoolings ($\geq -10^{\circ}\text{C}$),
264 goes no farther back than Mossop et al. 1970. One wishes some the earlier workers who
265 reported ice at unexpectedly high cloud top temperatures would have been cited in this first
266 grouping¹², such as Coons and Gunn 1951u; Ludlam 1955u; Murgatroyd and Garrod 1960u;
267 Borovikov et al. 1961u; Koenig 1963; Hobbs 1969u; Auer et al 1969u.

268 P 7.2, Section 2, F2017: “The consensus is that H-M occurs within a temperature range of
269 approximately -3°C to -8°C , in the presence of liquid cloud droplets smaller than $\sim 13\mu\text{m}$ and
270 liquid drops larger than $\sim 25\mu\text{m}$ in diameter that can freeze when they are collected by large ice
271 particles (rimed aggregates, graupel, or large frozen drops).”

272

273 It is now believed that the small droplets play a far less important role than once
274 envisioned. Goldsmith et al. (1976), later confirmed by Mossop (1978) appeared to find strong

¹² It has been said that references to ground breaking early work is disappearing in publications due to the presence of younger authors.

275 evidence that droplets $\leq 13\mu\text{m}$ diameter played a critical role in ice multiplication. In fact, it was
276 thought for a time that very low concentrations of those small drops would lead to clouds absent
277 in ice multiplication in clean locations (e.g., Hallett et al. 1980u). However, Mossop 1985a, u
278 himself, in later laboratory experiments determined that small drops played a much-reduced role
279 in H-M. Cloud studies in pristine environments where ice multiplication was rampant (RH91u
280 in the Washington State coastal waters in onshore flow, HR98 in the Arctic, Rangno and Hobbs
281 (2005) in the Marshall Islands, and Connolly et al. (2006a) in England, would seem to have
282 confirmed the minor role of droplets $\leq 13\mu\text{m}$ diameter in riming and splintering in clean
283 conditions.

284 Section 2, p7.3-7.4: The F2017 Table 1 and the discussion of laboratory and field observations
285 of secondary ice particles.

286 While Section 2 was remarkably thorough, some important findings were not cited, or
287 listed in Table 7.1 of the many studies of secondary ice particles. Ono (1971u, 1972u) should
288 have been included in Table 7-1 and in the accompanying F2017 discussions; he appears to have
289 preceded Hallett and Mossop (1974) concerning the importance of larger cloud droplets
290 coincident with graupel in ice multiplication¹³. Two elucidating quotes from Ono:

291 Ono (1971u), his abstract:

292 “(Ice crystal) sizes, concentrations and microphysical conditions of occurrence support
293 the hypothesis that they were formed when ice fragments were thrown off from water drops
294 freezing after accreting on ice crystals.”

¹³Ono worked with Mossop (e.g., Mossop and Ono 1969u), perhaps there was some “cross-pollination” of ideas...

295 Ono (1972u):

296 “However, from our present observations, it has been found that in the clouds where
297 moderately large drops of 30 to 60 μm in diameter and graupel-like rimed ice particles occurred
298 simultaneously, we have a high concentration of secondary ice crystals. The presence of drops
299 with some hundreds of microns in diameter is not a crucial factor for crystal multiplication.”

300 Moreover, Ono’s (1972u) findings above would appear to square better with our own
301 findings (e.g., HR90, RH91u) for maritime clouds in the Washington coastal waters concerning
302 high ice particle concentrations since our cumuliiform clouds in onshore flow always had plenty
303 of supercooled droplets $>30 \mu\text{m}$ diameter in their middle and upper portions, sizes that Ono
304 implicated in ice multiplication. Also, our Washington maritime clouds have virtually no mm-
305 sized drops as F2017 erroneously conclude are necessary for the “rapid” ice formation.

306 At the top of p 7.4: “...and observations are compromised by the potential of ice to break on
307 contact with the aircraft or instruments (e.g., Field et al. 2006).”

308 A single reference to Field et al (2006) regarding probe-related ice artifacts could lead the
309 reader to believe that shattering on probe tips was a very recently discovered problem.
310 Shattering on probe tips has been a well-known problem and was obvious in the imagery as soon
311 as 2D probes began to be used in the late 1970s. Those of us in airborne research have been
312 addressing this problem for more than 30 years to minimize the contribution of artifacts to ice
313 particle concentrations (e.g., Harris-Hobbs and Cooper 1987).

314 Many of reports of ice multiplication have originated at ground sites (e.g., Hobbs 1969u,
315 Auer 1969u, Burrows and Robertson 1969u, Ono 1971u, 1972u, Vardiman 1978). Citing these

316 reports and emphasizing that they were ground sites would have made it clear to the reader that
317 airborne artifacts have not reduced this enigma very much.

318 In fact, in view of the complexity of aircraft measurements of ice particles, MORE
319 ground observations are *critical*, particularly at sites where the H-M process should be frequently
320 active in clouds at the ground as in the Cascade Mountains of Washington State (e.g., Paradise
321 Ranger Station). Such ground measurements are vitally needed as well in the Middle East at
322 sites where there has been a dearth of ice-in-cloud measurements¹⁴. Some authors now claiming
323 that even modern outfitted research cannot derive accurate concentrations of ice particles (i.e.,
324 Freud et al. 2015). Hence, the need for more ground work if, in fact, the assertion in Freud et al.
325 2015 is true..

326 Section 2, last paragraph on p7.4: “Splinter production following the freezing of a large
327 millimeter size droplet that subsequently shatters (droplet shattering; e.g., Mason and Maybank
328 1960..”

329 The authors in citing Mason and Maybank (1960) several times are apparently unaware
330 that Mason and Maybank’s results were compromised by CO₂, as discovered by Dye and Hobbs
331 1966u. CO₂ is a gas that promoted the shattering of drops that Mason and Maybank observed.
332 Later, however, Hobbs and Alkesweeny 1968u, did find that a *few* splinters were shed by drops
333 that rotated in free fall as they froze, far fewer than reported by Mason and Maybank. Hobbs and
334 Alkesweeny’s work should have been cited along with that of Brownscombe and Thorndike

¹⁴ Sites to consider might be at Mt. Hermon, Israel, or at ski resorts in Lebanon. In-cloud situations with snow and graupel precipitation would be common at these sites.

335 (1968).

336 P7.2, Section 2, laboratory evidence for secondary ice formation:

337 The role of water supersaturation in ice formation was ignored as a possible source of
338 secondary ice. Gagin and Nozyce 1984u reported the appearance of ice crystals in the
339 environment of freezing mm-sized drops in lab experiments. They attributed the formation of
340 the new ice crystals to a pulse of high supersaturation with respect to water as the freezing drop
341 warmed to 0°C in their chamber. This could be an important secondary ice-forming mechanism,
342 similar in effect to that used by Chisnell and Latham (1976), who incorporated splinters derived
343 from freezing drops. This process might explain the simultaneous appearance of ice splinters
344 that appear so quickly, side-by-side, with frozen precipitation-sized drops.

345 P7.4, Section 3. In situ observations of SIP and the discussion of the role of IN.

346 The work of Rosinski (1991u) goes uncited. Rosinski did a lot of work on maritime IN,
347 ones that he claimed were active at slightly supercooled temperatures in concentrations of tens
348 per liter. His work should have been mentioned, even if it's only to state that his measurements
349 are not generally accepted. However, if he was even partially correct, his findings would go a
350 long way to explaining the rapidity of ice development in maritime clouds.

351 P7.5, “In addition, the measurements may be affected by the possibility that ice particles
352 generated by the passage of the aircraft through the cloud (Woodley et al. 2003) from previous
353 cloud passes could have mixed into the measured samples.”

354 The authors only cite Woodley et al. (2003) regarding aircraft-produced ice due to the
355 passage of an aircraft. This unexpected phenomenon was first reported 20 years prior to

356 Woodley et al. by Rangno and Hobbs (1983u, 1984u)¹⁵. Scientific etiquette requires that those
357 who went first be cited. Not citing benchmark papers that roiled the airborne research
358 community due to the temperatures at which ice was produced ($>-10^{\circ}\text{C}$) is remarkable. John
359 Hallett (2008) termed this finding, “an embarrassment to the airborne research community.”

360 Too, not being cited when you should be inflicts material damage since one’s impact in
361 one’s field, likelihood of promotions, awards, etc, is measured by citation metrics.

362 P7.6 “Lawson et al. (2015) suggest that the rapid glaciation in these strong updraft cores ($\sim 10\text{ms}^{-1}$)
363 occurs at temperatures too cold and too fast to be attributable to the H-M process.”

364 Citing the report of Stith et al. (2004u) would have been *perfect* here, as would have been
365 Paluch and Breed (1984u).

366 P7.7, discussion of Heymsfield and Willis (2014): “Heymsfield and Willis (2014) found that SIP
367 evidenced by observations of needles–columns throughout the range -3°C to -14°C was observed
368 predominantly where the vertical velocities were in the range from -1 to $+1\text{ms}^{-1}$. The LWCs in
369 the regions where SIP are observed are dominantly below 0.10gm^{-3} . Median LWCs in these
370 regions were only about 0.03gm^{-3} with no obvious dependence on the temperature.”

¹⁵ Our first two submitted manuscripts, ones that preceded RH83u, were rejected. The editor, B. Silverman wrote, concerning the 2nd manuscript, “The reviewers are still unconvinced by these controversial claims

371 The Heymsfield and Willis (2014) finding is not only counter to most of the Washington
372 experience but also that of other workers (e.g., Mossop et al. 1968u, Figure 4¹⁶; Mossop et al.
373 (1972u, Figure 2; Mossop 1985u, Figure 1), Paluch and Breed 1984u; Lawson et al 2015’s “first
374 ice”). Why? The initiation and observation of small ice particles in high concentrations usually
375 occurs in the higher (short-lived) LWC zones ($\geq 0.5 \text{ g m}^{-3}$). These contrary findings are not
376 mentioned by F2017, ones that would have presented a different picture of the origin of the high
377 concentrations of ice. Perhaps Heymsfield and Willis (2014) encountered their high ice particles
378 in cloud “death throes”; evaporating anvil shelving, rather having encountered them close to
379 where they formed?

380 P7.7, discussion of Taylor et al. (2016): “Taylor et al. (2016) analyzed aircraft measurements in
381 maritime cumulus with colder (11°C) cloud-base temperatures that formed over the southwest
382 peninsula of the United Kingdom. They found that almost all of the initial ice particles were
383 frozen drizzle drops [;(0.5–1) mm], whereas vapor-grown ice crystals were dominant in the later
384 stages. Their observations indicate that the freezing of drizzle–raindrops is an important process
385 that dominates the formation of large ice in the intermediate stages of cloud development. In the
386 more mature stage of cloud development the study found high concentrations of small ice within
387 the H-M temperature range.”

388 Virtually identical findings to Taylor et al.’s was reported for even cooler based clouds a
389 quarter of a century earlier by RH91u which should have been cited along with Taylor et al.’s.

¹⁶ Mossop et al. 1968u also found columnar ice particles in dissipating, anvil-like regions as well as in high LWC zones.

390 P7.7, 2nd: “It has been speculated that graupel does not need to play the rimer role. In situ
391 observations from frontal cloud systems suggest that riming snowflakes may be able to mediate
392 the SIP (Crosier et al. 2011; Hogan et al. 2002.)

393 The 2002 and 2011 references to non-graupel ice particles shedding splinters seem out of
394 place since this was considered so many years prior to these references. For example, riming by
395 other than graupel particles was part of the “potential” H-M scheme of Harris-Hobbs and Cooper
396 in 1987, in Mason 1998, and by Mossop 1985b.

397 P7.8. last three lines: “Finally, it should be noted that conditions where cloud tops are -12°C and
398 drizzle-sized supercooled droplets are present do not always result in the production of large
399 numbers of ice crystals. Bernstein et al. (2007) and Rasmussen et al. (1995) identified these
400 conditions as long-lived clouds and hazardous for aircraft.”

401 Some elaboration on the interesting and important findings of Bernstein et al. (2007) and
402 Rasmussen et al. (1995):

403 The University of Washington aircraft observed drizzle drops aloft in orographic clouds
404 in the Oregon Cascade Mountains during IMPROVE 2 (Stoelinga et al. 2003); we had not
405 observed them in the more aerosol-impacted clouds of the Washington Cascades in many years
406 of sampling them, though we did not fly in the kind of strong synoptic situations encountered in
407 IMPROVE 2.

408 However, those Oregon drizzle drops that we encountered in IMPROVE 2, as usually
409 happens, didn’t make it to the ground as liquid drops. IMPROVE 2 had ground measurements
410 in support of airborne work; no freezing rain or drizzle events were reported, a finding
411 compatible with long term records in the Sierras, and Cascades with precipitation at below

412 freezing temperatures under westerly flow situations and when the temperature decreases with
413 height (unpublished data). There is a duration-below-freezing-temperature factor, as well as the
414 temperature itself, that together control the freezing of precipitation-sized drops. The deeper the
415 sub-freezing layer at temperatures below about -4°C , the more likely drops will freeze on the
416 way down becoming sleet/ice pellets.

417 Supercooled layered cloud tops, sometimes colder than -30°C , are common and
418 persistent, and they have been known about since 1957 (Cunningham 1957u, Hall 1957u; this
419 situation is shown in Byers 1965u), and were described later by HR85, HR98, and explained by
420 Rauber and Tokay 1991u. Supercooled tops, usually ones having a broad droplet spectrum if
421 they are shedding ice (RH85), persist because the ice that forms within them falls out, as do
422 precipitation-sized drops, if any, and those drops freeze on the way down. Altocumulus clouds
423 sporting virga is a common example of this phenomenon. In this “upside down” storm situation,
424 ice particle concentrations have been observed to increase downward (e.g., HR85; Rasmussen et
425 al. 1995) likely due to the breakup of fragile crystals. This phenomenon can mislead researchers
426 solely using satellite data to infer the phase of entire cloud systems below those liquid tops.

427 p7.15, Section 6, discussion and conclusions section, second bulleted item: “The onset of the
428 rapid glaciation of convective clouds is observed to occur shortly after millimeter-size drops
429 freeze.”

430 If Ono’s 1972u findings are correct the glaciation process is also triggered by drops
431 smaller than even drizzle drops whose sizes range officially from 0.2 to 0.5 mm diameter. In our
432 cool-based, modest-sized Washington State maritime clouds (bases rarely $>6^{\circ}\text{C}$) with mm-sized
433 drops were rarely encountered; nevertheless, ice formation was usually rapid and prolific.

434 P7.15, Section 6, 2nd paragraph, last sentence: “It has been suggested by, for example, Koenig
435 (1963) and Lawson et al. (2015) that supercooled raindrops play an important role in the
436 initiation of the glaciation process and there is evidence that this can occur at temperatures
437 greater than -10°C.”

438 The phrasing that “there is evidence”, which was likely unintentional, makes it sound like
439 the appearance of ice in clouds with tops $\geq -10^{\circ}\text{C}$ is a rare phenomenon which the authors know
440 is hardly rare! It happens globally over the oceans in clean conditions, and in continental
441 convective clouds with warm bases.

442 P7.6 “Figure 7-6 shows aircraft observations taken within a few hundred meters of cloud top by
443 repeatedly penetrating a rapidly growing convective plume”

444 Can the authors rule out aircraft production of ice?

445 P7.7: “They found that almost all of the initial ice particles were frozen drizzle drops $\sim (0.5\text{--}1)$
446 mm], whereas vapor-grown ice crystals were dominant in the later stages.”

447 Drizzle drops are defined by the AMS and WMO as *close together* drops between 0.2
448 mm and 0.5 mm diameter. They virtually float in the air. The 0.5 to 1 mm diameter drops that
449 F2017 refer to are raindrops, not drizzle ones.

450 P7.2, Section 2, Laboratory Studies:

451 Amid citations of laboratory experiments that “have produced secondary ice”, we point
452 out that Choulaton et al (1980) only produced protuberances and spicules, not actual ice
453 particles. Later, F2017 again cite Choulaton et al. a bit incorrectly by suggesting the drop sizes

454 for spicule production he studied was “ $>\sim 25\ \mu\text{m}$ ”. Choularton et al. reported the main increase
455 in protuberances was for droplets $>20\ \mu\text{m}$ diameter.

456 P 7.4, Section 3, In Situ Cloud Studies, first paragraph, 2nd line: “Ice particles are often observed
457 in abundance in convective clouds that are colder than 0°C but with cloud-top temperatures
458 warmer than about -12°C ...”

459 Slightly more accurately: “... clouds whose tops have ascended past -4°C but have not
460 been colder than about -12°C ...”

461 P7.5, Section 3, last paragraph: “Hobbs and Rangno (1985, 1990, 1998), in a series of aircraft
462 investigations of maritime cumulus off the coast of Washington...”

463 F2017 indicates that HR98 concerned Washington State coastal clouds. It concerned
464 Arctic stratiform clouds sampled mainly over the Beaufort Sea. This seems like a remarkable
465 error for 29 authors to make. Moreover, in HR98 we discussed ice multiplication in pristine,
466 slightly supercooled Arctic Stratus clouds with extremely low ($<20\ \text{cm}^{-3}$) droplet concentrations.
467 We found little correlation between droplets $<13\ \mu\text{m}$ diameter droplets and small (≤ 300 diameter)
468 ice particles as some have reported (Harris-Hobbs and Cooper 1987) in support of their
469 importance in riming and splintering process. Yet ice was plentiful (10s per liter) regardless of
470 the concentrations of those small droplets in boundary-layer Stratocumulus clouds with tops of
471 just -4° to $-6^\circ\ \text{C}$.

472 P7.5, Section 3, the discussion of Harris-Hobbs and Cooper 1987: “Harris-Hobbs and Cooper
473 (1987) used airborne observations from cumulus clouds in three different geographic regions to
474 estimate secondary ice production rates.”

475 The California clouds that HHC87 examined were not Cumulus but were long stretches
476 of orographic stratiform, banded cloud systems.

477 Editorial note concerning the popular phrasing, “warm or “cold” temperatures in numerous
478 places.

479 A quote from Peter Hobbs on this common error; “A cup of coffee can be warm or cold,
480 but not a temperature.” A temperature is a number and can have no physical state itself, but
481 rather refers to the state of a tangible object.

482

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485 Washington, Seattle. He allowed me to become the most I could be in my field. This is also
486 dedicated to our “can do” pilots; the many members of our flight crews; our software engineers,
487 whose dedication to their jobs over the years in the adverse conditions that we often flew in,
488 made our findings possible.

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